

Hillside Township School District

Mathematics Department
Precalculus CP

Grades 11

Dr. Antoine L. Gayles
Superintendent of Hillside Public Schools

Dr. Christy Oliver-Hawley
Director of Curriculum and Instruction

Curriculum Contributors:
Mr. Emenaka, Mr. Thomas

Supervisor
Obinna Emenaka

Board of Education Approved:
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District Mission Statement

The mission of the Hillside Public Schools is to ensure that all students at all grade levels achieve the New Jersey Core Curriculum Content Standards and make connections to real-world success. We are committed to strong parent-community school partnerships, providing a safe, engaging, and effective learning environment, and supporting a comprehensive system of academic and developmental support that meets the unique needs of each individual.

Academic Area Overview

The Hillside Township School District is committed to excellence. We believe that all children are entitled to an education that will equip them to become productive citizens of the twenty-first century. We believe that a strong foundation in mathematics provides our students with the necessary skills to become competent problem solvers and pursue math intensive careers in the sciences and engineering.

A strong foundation in mathematics is grounded in exploration and rigor. Children are actively engaged in learning as they model real-world situations to construct their own knowledge of how math principles can be applied to solve every day problems. They have ample opportunities to manipulate materials in ways that are developmentally appropriate to their age. They work in an environment that encourages them to take risks, think critically, and make models, note patterns and anomalies in those patterns. Children are encouraged to ask questions and engage in dialogue that will lead to uncovering the math that is being learned. Facts and procedures are important to the study of mathematics. In addition to learning the common facts and procedures that lead efficient solutions of math problems, children will also have the opportunity to explore the “why” so that they can begin to understand that math is relevant to the world.

Our program provides teachers with resources both online and in print that incorporates the use of technology to help students reach the level of rigor that is outlined in the Common Core State Standards for Mathematics. Textbooks and materials have been aligned to the standards and teachers are trained on an ongoing basis to utilize the resources effectively and to implement research-based strategies in the classroom.

Affirmative Action Statement Equality and Equity in Curriculum

The Hillside Township School District ensures that the district’s curriculum and instruction are aligned to the State’s Core Curriculum Content Standards and addresses the elimination of discrimination and the achievement gap, as identified by underperforming school-level AYP reports for State assessment, by providing equity in educational programs and by providing opportunities for students to interact positively with others regardless of race, creed, color, national origin, ancestry, age, marital status, affectional or sexual orientation, gender, religion, disability or socioeconomic status.

N.J.A.C. 6A:7-1.7(b): Section 504, Rehabilitation Act of 1973; N.J.S.A. 10:5; Title IX, Education Amendments of 1972

Math Department Lesson Plan Template

Lesson Information

Lesson Name: _____

Unit: _____

Date: _____

Lesson Data

1. Essential Questions &
Enduring Understanding:

2. CCSS:

3. Knowledge:

4. Skills:

5. Informal/Formal
Assessment of Student
Learning:

6. Lesson Agenda:

7. Homework:

UNIT 1: Algebra Review

ENDURING UNDERSTANDINGS		ESSENTIAL QUESTIONS
<ul style="list-style-type: none"> ✓ Equations and inequalities can describe, explain, and predict various aspects of the real world. ✓ Change in Algebra can be represented using slope as the ratio of vertical change to horizontal change. ✓ A line on a graph can be represented by a linear equation. ✓ Systems of linear equations can be used to model real world problems. ✓ A single quantity can be represented by different polynomial expressions that follow the properties of real numbers. 		<ul style="list-style-type: none"> ✓ How can we use equations or inequalities to model the world around us? ✓ How can we represent rates of change algebraically? ✓ When is it possible to set up a system of equations to model a real problem? ✓ How do the properties of real numbers apply to polynomial expressions?
CCSS	KNOWLEDGE	SKILLS
Solving Equations & Inequalities A-CED1 A-CED4 A-REI1 A-REI3 A-REI10	Students will know that: <ul style="list-style-type: none"> • A variable can be used to represent a number in context. Any expressions, equations, or inequalities created using this variable must follow the properties of real numbers. • The properties of real numbers can be extended to formulas. 	Students will be able to: <ul style="list-style-type: none"> • Create equations and inequalities in one variable and use them to solve problems. Include equations arising from linear situations. • Rearrange formulas to highlight a quantity of interest, using the same reasoning as in solving equations. For example, Distance <p>Formula: $D = R \cdot T$ or $T = \frac{D}{R}$ or $R = \frac{D}{T}$</p>

	<ul style="list-style-type: none"> • In solving linear equations the properties of real numbers can be used to simplify the original equation and ensure that the equality of an expression is maintained from the previous step to the next step in the process. • To solve any linear equation or inequality, one must use the properties of real numbers to move variables on one side and numbers on the other side. 	<ul style="list-style-type: none"> • Solve linear equations and inequalities in one variable, including equations with coefficients represented by letters. • Explain each step in solving a simple equation as following from the equality of numbers asserted at the previous step, starting from the assumption that the original equation has a solution. Construct a viable argument to justify a solution method.
Slope, Linear Functions, Linear Inequalities & Their Graphs A-CED2 F-IF6 A-CED3	Students will know that: <ul style="list-style-type: none"> • The <u>slope</u> is a constant rate of change that measures steepness of a line - the higher the slope, the steeper the line. $\text{slope } (m) = \frac{\text{vertical change}}{\text{horizontal change}} = \frac{\text{rise}}{\text{run}} = \frac{y_2 - y_1}{x_2 - x_1}$ • The relationship between two lines can be determined by comparing their slopes and y-intercepts. 	Students will be able to: <ul style="list-style-type: none"> • Calculate the slope of a line using the formula or by analyzing the graph of a linear function. • Calculate and interpret the average rate of change of a function (presented symbolically or as a table) over a specified interval. Estimate the rate of change from a graph.
	<ul style="list-style-type: none"> • Linear equations can be written in the following forms: <ul style="list-style-type: none"> ○ Slope-Intercept Form: $y = mx + b$ ○ Point-Slope Form: $y - y_1 = m(x - x_1)$ ○ Standard Form: $Ax + By = C$ 	<ul style="list-style-type: none"> • Create equations in two variables to represent relationships between quantities; graph equations on coordinate axes (with labels & scales)
	<ul style="list-style-type: none"> • The graph of an inequality in two variables is the set of all of its solutions plotted on the coordinate plane and is represented by a half plane. 	<ul style="list-style-type: none"> • Graph the solutions to a linear inequality on a coordinate plane.

<p>Systems of Linear Equations & Inequalities</p> <p>A-REI5 A-REI6 A-REI11 A-REI10 A-REI12 A-CED3</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> • The solution of the system of equations is the intersection of the graphs of two functions. • Systems of equations can be solved by: <ul style="list-style-type: none"> ○ Graphing – The solution is the point of intersection of the lines. ○ Substitution – Replace one variable with the expression from the other equation. ○ Eliminating – Set up the coefficient of one of the variables to cancel by addition or subtraction of the equations. 	<p>Students will be able to:</p> <ul style="list-style-type: none"> • Graph two functions and find the solution which is the point(s) of intersection. • Find the solutions approximately, e.g. using technology to graph a function, make table of values, or find successive approximations. • Prove that manipulating two equations in a system using different operations or methods will produce equivalent equations and same solutions. • Represent constraints by equations and by systems of equations and interpret solutions as viable or nonviable options in a modeling context. <i>For example, finding the value when expenses equal income.</i>
	<ul style="list-style-type: none"> • The graph of a system of linear inequalities in two variables is the intersection of the corresponding half planes. 	<ul style="list-style-type: none"> • Graph the solutions to a linear inequality in two variables as a half plane and graph solution sets to a system of linear inequalities in two variables. • Represent constraints by inequalities, and by systems of inequalities, and interpret solutions as viable or nonviable options in a modeling context. <i>For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.</i>
<p>Operations on Polynomials, Factoring & Solving Quadratic Equations</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> • Polynomials form a system similar to the integers, namely, they are <u>closed</u> under the operations of addition, subtraction, and multiplication. <ul style="list-style-type: none"> ○ A polynomial is <u>closed</u> under the operation if the output is in the same set of numbers as the input. 	<p>Students will know that:</p> <ul style="list-style-type: none"> • Add, subtract, and multiply polynomials. • Use the properties of exponents to transform expressions • Combine like terms and evaluate algebraic expressions.

A-SSE2 A-SSE3 A-APR3 A-REI4	<ul style="list-style-type: none"> Polynomials can be factored into equivalent forms to reveal characteristics about the expression as well as to make equation solving simpler. <ul style="list-style-type: none"> Many quadratic expressions can be factored to yield the product of two linear expressions. 	<ul style="list-style-type: none"> Find the binomial factors of a quadratic trinomial and use its factors to find the zeros.
	<ul style="list-style-type: none"> The zeros of a function can be found graphically or algebraically by: <ul style="list-style-type: none"> Finding the x-intercepts on a graph. Setting the function to zero, factoring, and solving algebraically. $x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$ <ul style="list-style-type: none"> Using the quadratic formula: 	<ul style="list-style-type: none"> Solve quadratic equations by inspection, taking square roots, completing the square, the quadratic formula, and factoring, as appropriate to the initial form of the equation.
<u>Critical Vocabulary:</u> Variable, Expression, Real Number, Coefficient, Constant, Formula, Inequality, Equation, Coordinate Plane, Axis, Rate of Change, Slope, Function Notation, Linear, Quadratic, Exponential, y-intercepts, Inequality, Half Plane, System, Solution, Closed, intercepts, zero, roots, term, degree, monomial, binomial, trinomial, polynomial, factor, quadratic, complex numbers, imaginary numbers,		

Pacing Chart
UNIT 2: Modeling with Functions

TIME FRAME	TOPIC	SUGGESTED PERFORMANCE TASKS ACTIVITIES/PROJECTS ASSESSMENTS	RESOURCES/INTERDISCIPLINARY CONNECTIONS
1 st Week in Sept	Solving Equations & Inequalities	<p>Geology Rocks (Group Activity) http://illuminations.nctm.org/LessonDetail.aspx?id=L786 Graphing calculator utility http://my.hrw.com/math06_07/nsmedia/tools/Graph_Calculator/graphCalc.html Solving Equation - Games www.shodor.org/interactivate/activities/AlgebraFour National Library of Virtual Manipulatives http://nlvm.usu.edu/en/nav/topic_t_2.html Algebraic Balance Scales http://nlvm.usu.edu/en/nav/frames_asid_201_g_3_t_2.html?open=instructions&from=category_g_3_t_2.html Solving linear equations & inequalities: Games, lessons, reference sheet, dictionary and more. www.coolmath.com/algebra/algebra-practice-solving.html</p>	<p>Text Sections: P-3, P-5, P-7</p> <p>Teacher resources have activities, videos, projects, & enrichment.</p> <p>www.khanacademy.com</p> <p>www.teachertube.com</p> <p>exchange.smarttech.com</p>
2 nd Week in Sept	Slope, Linear Functions, Linear Inequalities & Their Graphs	<p>Chapter 5 Project Slope Millionaire game http://www.quia.com/rr/79713.html Slope Jeopardy http://www.quia.com/cb/24707.html Virtual Slope (slope slider) http://www.shodor.org/interactivate/activities/SlopeSlider/ Linear equation Activities/Games/Projects http://www.ilovemath.org/index.php?option=com_docman&task=cat_view&gid=55&dir=DESC&order=date&limit=10&limitstart=20 Slope Intercept Rap</p>	<p>Text Sections: P-4</p> <p>Teacher resources have activities, videos, projects, & enrichment.</p> <p>www.khanacademy.com</p> <p>www.teachertube.com</p> <p>exchange.smarttech.com</p>

		http://www1.teachertube.com/viewVideo.php?video_id=101097 Linear inequalities millionaire http://www.quia.com/rr/79715.html	
3 rd Week in Sept	Systems of Linear Equations & Inequalities	System of Equations Activities http://www.ilovemath.org/index.php?option=com_docman&task=cat_view&gid=53 More Systems Activities http://player.discoveryeducation.com/index.cfm?guidAssetId=41BD9CF7-7138-46E9-A81B-BB0E01B7526A&blnFromSearch=1&productcode=US Systems Jeopardy http://www.quia.com/cb/79607.html Solving systems of equations basketball game http://www.crctlessons.com/systems-of-equations-game.html System of Equations Activities http://www.ilovemath.org/index.php?option=com_docman&task=cat_view&gid=53 Linear inequality millionaire http://www.quia.com/rr/79715.html	Text Sections: 7-1, 7-5, Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com
Last Week in Sept	Operations on Polynomials, Factoring & Solving Quadratic Equations	More practice with polynomials http://www.coolmath.com/algebra/algebra-practice-polynomials.html Sorting poly by type http://www.enotes.com/documents/polynomial-sort-42283 Polynomial bingo http://makingmathfun.wikispaces.com/file/view/Polynomial+Factoring+Bingo.pdf Factoring (Various Topics) http://www.geneyang.com/factoring/main.swf Quadratic equations matching game http://www.studystack.com/matching-4767 Solving Quadratic equations Webquest http://www.rblewis.net/technology/EDU506/WebQuests/quadratics/quadratics.html	Text Sections: P-5, P-6, P-7, 1-1 Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com

		<p>Polynomial Activity on making connections between polynomial functions and the graphs of these functions http://illuminations.nctm.org/LessonDetail.aspx?id=L282</p> <p>Graphing Quadratic functions http://education.ti.com/calculators/downloads/US/Activities/Detail?id=6655&ref=%2fcalculators%2fdownloads%2fUS%2fActivities%2fSearch%2fSubject%3fs%3d5022%26sa%3d5022%26t%3d5035%26d%3d2</p> <p>Graphing Quad Functions http://education.ti.com/calculators/downloads/US/Activities/Detail?id=9406</p> <p>Quadratic Formula Song http://education.ti.com/calculators/downloads/US/Activities/Detail?id=9406</p>	
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UNIT 2: Modeling With Functions and Their Graphs

ENDURING UNDERSTANDINGS		ESSENTIAL QUESTIONS
<ul style="list-style-type: none"> ✓ Polynomial functions allow us to model real world applications found in various mathematical disciplines. ✓ An understanding of the mathematics behind fractions and polynomials can help in making sense of rational expressions. ✓ Sometimes solving equations correctly results in answers that are incorrect and must be checked. ✓ Functions can be used to model relationships both real world and abstract. ✓ Different types of functions can be identified by their graphs. ✓ Exponential functions can be used to model situations involving rapid growth or decay. ✓ Changes to a function in algebraic form result in predictable changes to its graph. ✓ Systems of equations and inequalities allow us to organize information to make informed decisions and solve complex problems. 		<ul style="list-style-type: none"> ✓ When does it make sense to use a polynomial function to model a situation? ✓ What are the similarities between working with basic fractions and working with rational expressions? Differences? ✓ Why are answers that are derived using correct methods actually incorrect? ✓ How can various graphical and algebraic methods be used to analyze functions? ✓ Why is it that none of the previously learned functions could model exponential growth or decay? ✓ Why do changes in the graph of a function occur when we change the function using arithmetic operations? ✓ How can graphical and analytical methods be used to support each other in solving non-linear systems? ✓ How does an understanding of linear systems help in solving non-linear systems?
CCSS	KNOWLEDGE	SKILLS

<p>Relations & Functions</p> <p>F-IF1 F-IF2 F-IF3 F-IF5 F-IF7 F-BF1 F-BF2 A-CED2</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> A <u>relation</u> is a relationship between two sets of information that is represented by an ordered pair (x, y). <ul style="list-style-type: none"> A <u>function</u> is a special relationship between two sets of information in which every element from one set (domain) is paired with exactly one element in another set (range). The <u>domain</u> is the set of all allowable input values for a relation or function. The <u>range</u> is the set of all possible output values for a relation or function. 	<p>Students will be able to:</p> <ul style="list-style-type: none"> Identify the domain and range of a given relation or function. Recognize a function from a table of order pairs, input/output <i>mapping diagram</i>, and graph (vertical line test). Select the appropriate domain to represent a given situation.
	<ul style="list-style-type: none"> The graph of a relation or function is the set of all ordered pairs plotted on the coordinate plane. 	<ul style="list-style-type: none"> Graph a function within a given domain or range. Relate the domain of a function to its graph and where applicable to the quantitative relationship it describes. For example if a function $h(n)$ gives the number of person-hours it takes to assemble an engine in a factory, then the positive integers would be an appropriate domain for the function.
	<ul style="list-style-type: none"> Function notation is denoted by the symbol $f(x)$ to which f depends on the value of x. The graph of f is the graph of the equation $y = f(x)$. 	<ul style="list-style-type: none"> Use function notation to evaluate functions for inputs in their domains and interpret statements that use function notation in terms of a context. Write a function based on a given context.
	<ul style="list-style-type: none"> The operations of addition, subtraction, multiplication, division, and composition can be applied to functions. <ul style="list-style-type: none"> These operations can effect the domain of the resulting function. 	<ul style="list-style-type: none"> Apply the operations of addition, subtraction, multiplication, and division to various functions and identify the domain of the new function.
<p>Solving Polynomial Equations</p> <p>N.CN.7</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> Completing the square, factoring, or the quadratic formula can be used to solve quadratic equations with complex solutions. 	<p>Students will be able to:</p> <ul style="list-style-type: none"> Solve quadratic equations with real coefficients that have complex solutions. Create quadratic equations and inequalities in one variable and use

<p>N.CN.9 A.APR.3</p>	<ul style="list-style-type: none"> • The <u>Fundamental Theorem of Algebra</u> states that the number of complex solutions to a polynomial equation is equal to the degree of the polynomial. • The key features of a polynomial function can be observed on a graph. 	<p>them to solve problems.</p> <ul style="list-style-type: none"> • Show that The Fundamental Theorem of Algebra is true for quadratic polynomials. • Graph functions and show key features of the graph, by hand in simple cases or use technology for more complicated cases. <ul style="list-style-type: none"> ○ Graph polynomial functions, identifying zeros when suitable factorizations are available, and showing end behavior • Identify zeros of polynomials when suitable factorizations are available, and use the zeros to construct a rough graph of the function defined by the polynomial.
<p>Rational & Radical Expressions and Their Equations</p> <p>A.SSE.4 A.APR.7 A.REI.2</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> • An understanding of the basic rules of exponents can be used to simplify expressions and solve radical equations. • Radical equations may have extraneous solutions therefore all solutions must be checked by substituting into the original equation. <hr/> <ul style="list-style-type: none"> • Rational expressions form a system analogous to the rational numbers, closed under addition, subtraction, multiplication, and division by a nonzero rational expression. • The formula for the sum of a finite geometric series is: $S_n = \frac{g_1(r^n - 1)}{r - 1}$ <ul style="list-style-type: none"> ○ 	<p>Students will be able to:</p> <ul style="list-style-type: none"> • Solve simple rational and radical equations in one variable, and give examples showing how extraneous solutions may arise. <hr/> <ul style="list-style-type: none"> • Create equations in one variable and use them to solve problems involving simple rational functions. • Add, subtract, multiply, and divide rational expressions. • Derive the formula for the sum of a finite geometric series (when the common ratio is not 1), <ul style="list-style-type: none"> ○ Use the formula to solve problems. <ul style="list-style-type: none"> ▪ <i>For example, calculate mortgage payments.</i>
<p>Modeling & Graphs of Functions</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> • The graph of an equation in two variables is a visual representation of all possible solutions to the equation. 	<p>Students will be able to:</p> <ul style="list-style-type: none"> • Create equations in two or more variables to represent non-linear relationships between quantities.

<p>F.IF.7 A.CED.2 F.IF.4 F.IF.5 F.IF.6 F.IF.8 F.IF.9 F.BF.1 F.BF.4</p>	<ul style="list-style-type: none"> The key features of the following types of functions can be determined from graphical, numerical, or algebraic representations: <ul style="list-style-type: none"> Square root Cube root Absolute Value Piecewise defined Step The key features of functions are: <ul style="list-style-type: none"> Intercepts Intervals where the function is increasing, decreasing, positive, or negative Relative maximums and minimums Symmetries Odd/Even Functions End behavior Periodicity 	<ul style="list-style-type: none"> Graph the equations on coordinate axes with labels and scales. Graph functions expressed symbolically. Sketch graphs given a verbal description of the relationship. <ul style="list-style-type: none"> Show key features of the graph: <ul style="list-style-type: none"> By hand in simple cases Using technology for complex situations. Interpret key features of graphs and tables in terms of the quantities. Compare the key features of two functions each represented in different ways. <ul style="list-style-type: none"> <i>For example, given a graph of one quadratic function and an algebraic expression for another, say which has the larger maximum.</i>
	<ul style="list-style-type: none"> The average rate of change can be interpreted as the slope between two points on the graph of a function for a given interval. <ul style="list-style-type: none"> For non-linear functions, the average rate of change varies based on the interval given. $\text{Average Rate of Change} = \frac{f(b) - f(a)}{b - a}$ <ul style="list-style-type: none"> for the interval $[a, b]$ 	<ul style="list-style-type: none"> Calculate and interpret the average rate of change of a function over a specified interval algebraically, numerically and graphically.
	<ul style="list-style-type: none"> Different forms of a function reveal information about the function. <ul style="list-style-type: none"> Sometimes there is a need to write equivalent forms of a function based on the information required. 	<ul style="list-style-type: none"> Write a function defined by an expression in different but equivalent forms. <ul style="list-style-type: none"> <i>For example, changing a quadratic function from standard form to vertex form.</i>

	<ul style="list-style-type: none"> Domain restrictions on a function must be considered when applying functions to real world problems. 	<ul style="list-style-type: none"> Identify a reasonable domain for a function given its graph or the situation it describes. <ul style="list-style-type: none"> <i>For example, if the function $h(n)$ gives the number of person-hours it takes to assemble n engines in a factory, then positive integers would be an appropriate domain for the function.</i>
	<ul style="list-style-type: none"> Parts of a function have meaning and sometimes can be understood as separate functions combined together. 	<ul style="list-style-type: none"> Write a function that describes a relationship between two quantities. <ul style="list-style-type: none"> Combine standard function types using arithmetic operations. <ul style="list-style-type: none"> <i>For example, the cooling of an object over time can be modeled by combining a constant function and a decaying exponential function.</i>
	<ul style="list-style-type: none"> A function has an inverse that is a function if the relationship between inputs and outputs is one to one. Meaning: <ul style="list-style-type: none"> Each input is paired with exactly one output and each output is paired with exactly one input. 	<ul style="list-style-type: none"> Write an expression for an inverse function.
Exponential & Logarithmic Functions F.IF.7 F.LE.4	Students will know that: <ul style="list-style-type: none"> Exponential functions are in the form: <ul style="list-style-type: none"> $f(x) = ab^x$ where $b \neq 0$ 	Students will be able to: <ul style="list-style-type: none"> Create equations in one variable and use them to solve problems involving exponential functions.
	<ul style="list-style-type: none"> The solution to an exponential equation can be found using the properties of logarithms. <ul style="list-style-type: none"> The solution to $ab^x = d$ can be represented as $x = \log_b \left(\frac{d}{a} \right)$ a and d are numbers and the base, b is 2, 10, or e. 	<ul style="list-style-type: none"> Use their understanding of the relationship between exponential functions and logarithms to solve exponential equations. <ul style="list-style-type: none"> <i>Evaluate the logarithm using technology.</i>

	<ul style="list-style-type: none"> The key features of functions are: <ul style="list-style-type: none"> Intercepts End behavior 	<ul style="list-style-type: none"> Graph exponential and logarithmic functions by hand in the simple cases and using technology for more complicated cases.
Transformations on Functions F.BF.3	Students will know that: <ul style="list-style-type: none"> Given a function $f(x)$, each of the following manipulations to the function results in a physical transformation to the shape of the graph: <ul style="list-style-type: none"> $f(x) + k$ $f(x + k)$ $k \cdot f(x)$ $f(kx)$ k can be any positive or negative real number. 	Students will be able to: <ul style="list-style-type: none"> Experiment through the use of graphing technology to come to conclusions about transformations on functions. Identify the effects on the graph of a function based on algebraic manipulations of the function rule.
Non-linear Systems and Linear Programming A.REI.11 A.CED3	Students will know that: <ul style="list-style-type: none"> The x-coordinates of the point(s) where the graphs of the equations $y = f(x)$ and $y = g(x)$ intersect are the solution(s) of the equation $f(x) = g(x)$. Including cases where the functions are: <ul style="list-style-type: none"> Linear, Polynomial, Rational, Absolute value, Exponential, or Logarithmic 	Students will be able to: <ul style="list-style-type: none"> Approximate the solutions of systems of non-linear functions by: <ul style="list-style-type: none"> Using technology to graph the functions Making tables of values Finding successive approximations.
	<ul style="list-style-type: none"> Knowledge of systems of equations/inequalities can aid in making decisions when solving complex problems. Sometimes the solutions to a system of equations/inequalities are not viable answers to the problem in context. 	<ul style="list-style-type: none"> Represent constraints by equations or inequalities, and by systems of equations and/or inequalities, and interpret solutions as viable or non-viable options in a modeling context. <i>For example, represent inequalities describing nutritional and cost constraints on combinations of different foods.</i>
	<u>Critical Vocabulary:</u> Functions: Linear, Polynomial, Absolute Value, Exponential, Logarithmic, Piecewise Defined, Step, Inverse), Constraints, Systems of Equations, Formulas, Domain, Average Rate of Change, Interval, Equivalent, Real Numbers, Complex Numbers, Terms, Expression, Coefficient, Constant, Polynomial, Degree, Closed, Factor, Remainder, End Behavior, Equation, Zeros, Radical, Rational, Finite Geometric Series, Common Ratio, Extraneous	

	Solution, closed under an operation,
Common Midterm Exam:	

Pacing Chart
UNIT 2: Modeling with Functions

TIME FRAME	TOPIC	SUGGESTED PERFORMANCE TASKS ACTIVITIES/PROJECTS ASSESSMENTS	RESOURCES/INTERDISCIPLINARY CONNECTIONS
Early Oct – End of Oct	Relations & Functions	Relations & Functions Activities http://www.mathwarehouse.com/algebra/relation/ Function machine http://nlvm.usu.edu/en/nav/frames_asid_191_g_3_t_1.html	Text Sections: 1-2, 1-4, Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com
End of Oct – Mid Nov	Solving Polynomial Equations	Online calculator to find the roots of a polynomial http://easycalculation.com/algebra/algebra.php Online polynomial long division calculator http://calc101.com/webMathematica/long-divide.jsp Online calculators and solvers http://www.mathportal.org/calculators.php	Text Sections: 2-4, 2-5, Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com

Mid Nov – Early Dec	Rational & Radical Expressions and Their Equations	<p>In-class activity on rational expressions http://www.casioeducation.com/resource/pdfs/unit02.pdf</p> <p>Simplify radical expressions online calculator – square roots only http://www.mathportal.org/calculators/radical-expressions/simplifying-radical-expressions.php</p> <p>Online calculators and solvers http://www.mathportal.org/calculators.php</p> <p>Activity on radicals http://www.brainmass.com/math/algebra/163179</p>	<p>Text Sections: 2-6, 2-7,</p> <p>Teacher resources have activities, videos, projects, & enrichment.</p> <p>www.khanacademy.com</p> <p>www.teachertube.com</p> <p>exchange.smarttech.com</p>
Early Dec – Winter Break	Modeling & Graphs of Functions	<p>Tutorial on Functions and Models. Talks about Cost, revenue and profit http://www.zweigmedia.com/RealWorld/tutorialsf0/framesF2A.html</p> <p>The Graph of a Function http://www.intmath.com/functions-and-graphs/4-graph-of-function.php</p> <p>Discusses the graphing of some more complex functions http://www.analyzemath.com/Graphing.html</p> <p>Graphing tool for modeling functions http://hs-mathematics.wikispaces.com/Rational+Functions</p> <p>Linear and Nonlinear Functions http://www.glencoe.com/sec/math/prealg/prealg05/study_guide/pdfs/prealg_pssg_G112.pdf</p> <p>YouTube video comparing linear and nonlinear functions http://www.youtube.com/watch?v=_850e1mEiD4</p> <p>Discusses the reasonableness of the domain http://www.phschool.com/atschool/academy123/english/academy123_content/wl-book-demo/ph-147s.html</p> <p>Average rate of change http://www.mesacc.edu/~marfv02121/readings/average/index.html</p>	<p>Text Sections: 1-1, 1-2, 1-3, 1-5, 1-7, 2-1, 2-2, 2-3,</p> <p>Teacher resources have activities, videos, projects, & enrichment.</p> <p>www.khanacademy.com</p> <p>www.teachertube.com</p> <p>exchange.smarttech.com</p>

Early Jan – Mid Jan	Exponential & Logarithmic Functions	Discusses the graphing of some more exponential and logarithmic functions http://www.analyzemath.com/Graphing.html Various web-pages that support exponential and logarithmic functions http://www.intmath.com/exponential-logarithmic-functions/exponential-log-functions-intro.php	Text Sections: 3-1, 3-2, 3-3, 3-4, 3-5, 3-6, Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com
Mid Jan – End of Jan	Transformations on Functions	Transforming Functions http://regentsprep.org/Regents/math/algtrig/ATP9/funclesson1.htm	Text Sections: 1-6 Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com
End of Jan – Early Feb	Non-linear Systems and Linear Programming	http://www.dummies.com/how-to/content/how-to-solve-nonlinear-systems.html Examples and visuals of linear programming http://www.purplemath.com/modules/linprog3.htm	Text Sections: 7-1 Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com

UNIT 3: Right Triangle & Unit Circle Based Trigonometry

ENDURING UNDERSTANDINGS		ESSENTIAL QUESTIONS
<ul style="list-style-type: none"> ✓ An understanding of right triangles can aid in a variety of applications that may require indirect measurement. ✓ Defining trigonometric functions based on the unit circle provides a means of addressing situations that cannot be modeled with the tools of geometry. ✓ An understanding of coordinate geometry and functions are essential to the study of trigonometry. ✓ Trigonometric functions can be applied to areas of study involving periodic behavior. 		<ul style="list-style-type: none"> ✓ How can trigonometry be used to solve problems that involve indirect measurement and large distances? ✓ Why are radian measures used rather than degree measures in working with trigonometric functions and their applications? ✓ What prior knowledge is needed for understanding trigonometric functions and its uses? ✓ How can you model periodic behavior?
CCSS	KNOWLEDGE	SKILLS
Right Triangle Trigonometry G.SRT.6 G.SRT.7 G.SRT.8	Students will know that: <ul style="list-style-type: none"> • The Pythagorean Theorem states that the sum of the square of each leg of a right triangle equals the square of the hypotenuse. <ul style="list-style-type: none"> ○ $a^2 + b^2 = c^2$ • By similarity, side ratios in right triangles are properties of the angles in the triangle, leading to definitions of trigonometric ratios for acute angles. • The following trigonometric ratios are: <ul style="list-style-type: none"> ○ $\sin \theta = \frac{\textit{Opposite}}{\textit{Hypotenuse}}$ and $\csc \theta = \frac{1}{\sin \theta}$ ○ $\cos \theta = \frac{\textit{Adjacent}}{\textit{Hypotenuse}}$ and $\sec \theta = \frac{1}{\cos \theta}$ 	Students will be able to: <ul style="list-style-type: none"> • Use the Pythagorean Theorem along with any necessary trigonometric ratios to determine angles and side lengths in a right triangle as well as solve application problems. • Explain and use the relationship between the sine and cosine of complementary angles. • Use trigonometric ratios and the Pythagorean Theorem to solve right triangles in applied problems.

	$\tan \theta = \frac{\sin \theta}{\cos \theta} \text{ and } \cot \theta = \frac{1}{\tan \theta}$	
Unit Circle, Trigonometric Functions & Their Graphs F.TF.1 F.TF.2 F.TF.5 F.TF.8	Students will know that: <ul style="list-style-type: none"> The <u>Unit Circle</u> is a circle with a radius of one and center located at the origin. <ul style="list-style-type: none"> The unit circle can be used to represent various angle measures The <u>Radian</u> measure of an angle is the length of the arc on the unit circle subtended by the angle. <ul style="list-style-type: none"> Arc length is defined by equation $S = \theta r$ 	Students will be able to: <ul style="list-style-type: none"> Explain how the unit circle in the coordinate plane: <ul style="list-style-type: none"> Enables the extension of trigonometric functions to all real numbers Can be used to interpret radian measures of angles created from rotations around the unit circle.
	<ul style="list-style-type: none"> Points on the unit circle have an x-coordinate of $\cos \theta$ and a y-coordinate of $\sin \theta$. <ul style="list-style-type: none"> Ordered pairs can be written as $(\cos \theta, \sin \theta)$ The value of the cosine or sine can be positive or negative based on the quadrant. All six trigonometric functions can be computed for common angle measures without using a calculator (i.e. Trig function charts, special right triangles, unit circle) 	<ul style="list-style-type: none"> Use the unit circle to determine $\cos \theta$ and $\sin \theta$ for various angle measures. Determine the values of $\sin \theta$, $\cos \theta$, $\tan \theta$, $\csc \theta$, $\sec \theta$, and $\cot \theta$ for the following common angles and their multiples <u>without the use of a calculator</u>: <ul style="list-style-type: none"> $\theta = 0, \frac{\pi}{6}, \frac{\pi}{4}, \frac{\pi}{3}, \text{ and } \frac{\pi}{2}$ Use a trig functions chart of common angles and an understanding of the unit circle to evaluate all six trigonometric functions. Determine the value of $\sin \theta$, $\cos \theta$, or $\tan \theta$ given a value of any

		of the three trigonometric functions and a known quadrant.
	<ul style="list-style-type: none"> An inverse trigonometric function can be used to compute the value of an angle measure given the value of a trigonometric function <ul style="list-style-type: none"> $\sin^{-1} \theta$, $\cos^{-1} \theta$, $\tan^{-1} \theta$ 	<ul style="list-style-type: none"> Find the angle measure given the value of a trigonometric function.
	<ul style="list-style-type: none"> The Pythagorean Theorem can be used to prove trigonometric identities. 	<ul style="list-style-type: none"> Prove all three Pythagorean identity <ul style="list-style-type: none"> $\sin^2 \theta + \cos^2 \theta = 1$ $1 + \tan^2 \theta = \sec^2 \theta$ $\cot^2 \theta + 1 = \csc^2 \theta$ Use a Pythagorean Identity, a value for a trigonometric function, and a known quadrant to find any of the six trigonometric functions.

	<ul style="list-style-type: none"> Trigonometric functions have an amplitude, frequency and midline. <ul style="list-style-type: none"> $f(x) = A \sin(Bx + C) + D$ $f(x) = A \cos(Bx + C) + D$ <ul style="list-style-type: none"> The absolute value of A is the amplitude. The frequency is the number of full cycles in an interval (2π). $\text{frequency} = \frac{B}{2\pi}$ Phase shift is horizontal shift in the graph and is $\frac{C}{B}$ determined by the value and sign of $\frac{C}{B}$. The <u>Midline</u> is the horizontal line that passes through the middle of a trigonometric function. $y = \frac{\text{Max} + \text{Min}}{2}$ 	<ul style="list-style-type: none"> Graph trigonometric functions, showing period, midline, and amplitude. Choose a trigonometric function to model periodic behaviors with specified amplitude, frequency, and midline.
<p>Extensions of Trigonometry</p> <p>Laws of Sines and Cosines</p> <p>G.SRT.9 G.SRT.10 G.SRT.11</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> The Law of Sines and the Law of Cosines can be used to find unknown measurements in right and non-right triangles (e.g., surveying problems, resultant forces). 	<p>Students will be able to:</p> <ul style="list-style-type: none"> (+) Prove the Laws of Sines and Cosines and use them to solve problems. (+) Apply the Law of Sines and Cosines to find unknown measurements in both right and non-right triangles (+) Derive the formula $A = \frac{1}{2}ab \sin C$ for the area of a triangle by drawing an auxiliary line from a vertex perpendicular to the opposite side.

	<ul style="list-style-type: none">• Addition and subtraction formulas for the cosine and sine are<ul style="list-style-type: none">◦ $\cos(\alpha \pm \beta) = \cos \alpha \cos \beta \mp \sin \alpha \sin \beta$◦ $\sin(\alpha \pm \beta) = \sin \alpha \cos \beta \pm \cos \alpha \sin \beta$• Double angle formulas for the cosine and sine a<ul style="list-style-type: none">◦ $\sin 2\theta = 2 \sin \theta \cos \theta$◦ $\cos 2\theta = \cos^2 \theta - \sin^2 \theta = 2 \cos^2 \theta - 1 = 1 - 2 \sin^2 \theta$	<ul style="list-style-type: none">• Find the exact values of sine and cosine of uncommon angles that are the sum or difference of common angles without using a calculator.• Use the double angle formulas to prove trigonometric identities.
	<u>Critical Vocabulary</u> : Radian measure, Arc, Arc Length, Unit Circle, Trigonometric Functions, Inverse Trigonometric Functions, Real Numbers, Period, Periodic, Amplitude, Frequency, Midline, Pythagorean Identity, Sine, Cosine, Tangent, Law of Sines, Law of Cosines	
Common 1 st Quarter Assessment		

Pacing Chart
UNIT 3: Right Triangle & Unit Circle Based Trigonometry

TIME FRAME	TOPIC	SUGGESTED PERFORMANCE TASKS ACTIVITIES/PROJECTS ASSESSMENTS	RESOURCES/INTERDISCIPLINARY CONNECTIONS
Early Feb – Mid Feb	Right Triangle Trigonometry	Videos lessons of trigonometric concepts. http://wps.aw.com/aw_demana_precalculus_8/ Trigonometric relationships http://www.clarku.edu/~djoyce/trig/identities.html Supplemental practice problems in Trigonometry www.interactivemath.com Sample problems with solutions that show how to apply trigonometry for right triangles http://www.themathpage.com/atrig/solve-right-triangles.htm Interactive tool that explains the relationships in special right triangles http://www.mrperezonlinemath tutor.com/G/3_3_Using_30_60_90_and_45_45_90_ratios.html	Text Sections: 4-1, 4-2, 4-3, Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com
Mid Feb – End of Mar	Unit Circle, Trigonometric Functions & Their Graphs	Videos lessons of trigonometric concepts. http://wps.aw.com/aw_demana_precalculus_8/ Supplemental practice problems in Trigonometry www.interactivemath.com Information on the Law of Cosines http://en.wikipedia.org/wiki/Law_of_cosines Various tools for analysis of the unit circle & trigonometric identities http://www.explorelearning.com/index.cfm?method=cResource.dspResourcesForCourse&CourseID=254 Video on graphing trigonometric functions http://www.youtube.com/watch?v=80c_F0-7ZxE	Text Sections: 4-1, 4-3, 4-4, 4-5, 4-7, 4-8, 5-1, 5-2, Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com

End of Mar – Early Apr	Extensions of Trigonometry Laws of Sines and Cosines	<p>Videos lessons of trigonometric concepts. http://wps.aw.com/aw_demana_precalculus_8/ Supplemental practice problems in Trigonometry www.interactivemath.com Various tools for analysis of trigonometric identities http://www.explorelearning.com/index.cfm?method=cResource.dspResourcesForCourse&CourseID=254</p>	<p>Text Sections: 5-3, 5-4, 5-5, 5-6</p> <p>Teacher resources have activities, videos, projects, & enrichment.</p> <p>www.khanacademy.com</p> <p>www.teachertube.com</p> <p>exchange.smarttech.com</p>
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UNIT 4: Inferences and Conclusions from Data

ENDURING UNDERSTANDINGS		ESSENTIAL QUESTIONS
<ul style="list-style-type: none"> ✓ Normal distributions model many common, natural occurring phenomena. ✓ The way that data is collected determines the scope and nature of the conclusions that can be drawn from the data. ✓ Good statistical information about a population can be attained by studying a sample of the population. ✓ Probability models can be used to analyze situations and make fair decisions. 		<ul style="list-style-type: none"> ✓ Why do you think measurements with a bell-shaped distribution are so common in the world? ✓ What are the purposes of and differences among sample surveys, experiments, and observational studies? ✓ How can you ensure that a sample of a population is good enough to represent the population from which it was taken? ✓ How does the theoretical probability of an even occurring relate to the occurrence of the event? ✓ How can probability be used to make decisions fairly?
CCSS	KNOWLEDGE	SKILLS
Statistical Methods S-ID4 S-IC1 S-IC2	Students will know that: <ul style="list-style-type: none"> • Statistics is a collection of procedures and principles for gathering data and analyzing information in order to help people make decisions when faced with uncertainty. • Summation notation can be used to write the sum of quantities in a compact form and is useful in the study of both statistics and calculus. <ul style="list-style-type: none"> ○ Sums written in summations notation can be computed either algebraically or numerically. 	Students will be able to: <ul style="list-style-type: none"> • Make inferences about population parameters based on a random sample from that population. • Use simple algebra rules to compute the sums of quantities written in summation notation. <ul style="list-style-type: none"> ○ $\sum_{i=1}^n ca_i = c \cdot \sum_{i=1}^n a_i$ ○ $\sum_{i=1}^n (a_i + b_i) = \sum_{i=1}^n a_i + \sum_{i=1}^n b_i$ ○ $\sum_{i=1}^n (a_i - b_i) = \sum_{i=1}^n a_i - \sum_{i=1}^n b_i$ • Use special sum formulas to compute sums.

		<ul style="list-style-type: none"> o $\sum_{i=1}^n i = \frac{n(n+1)}{2}$ o $\sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}$ o $\sum_{i=1}^n i^3 = \left[\frac{n(n+1)}{2} \right]^2$ o $\sum_{i=1}^n i^4 = \frac{n(n+1)(6n^3 + 9n^2 + n - 1)}{30}$
	<ul style="list-style-type: none"> • The mean is the average of the data and the standard deviation is a measure of the spread of the data. <ul style="list-style-type: none"> o Mean for a sample is: $\bar{x} = \frac{\sum x_i}{n}$ o Standard deviation for a sample is: $s = \sqrt{\frac{\sum (x_i - \bar{x})^2}{n-1}} \quad \text{or} \quad s = \sqrt{\frac{\sum x_i^2 - n\bar{x}^2}{n-1}}$ • The following approximations can be made for a data set that is normally distributed: <ul style="list-style-type: none"> o 68% of the values fall within 1 standard deviation of the mean in either direction. o 95% of the values fall within 2 standard deviation of the mean in either direction. o 99.7% of the values fall within 3 standard deviation of the mean in either direction. 	<ul style="list-style-type: none"> • Use the mean and standard deviation of a data set to fit it to a normal distribution <ul style="list-style-type: none"> o Use the normal distribution to estimate population percentages. o Recognize that there are data sets for which this procedure is not appropriate. o Use calculators, spreadsheets, and tables to estimate areas under the normal curve.

<p>Data Analysis</p> <p>S-IC2 S-IC3 S-IC4 S-IC5 S-IC6</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> Data can be collected in different ways: <ul style="list-style-type: none"> Sample surveys Experiments Observational study Simulations <hr/> <ul style="list-style-type: none"> There is variability in experiments. Statistics is used as a way of dealing with, not eliminating, inherent randomness. 	<p>Students will be able to:</p> <ul style="list-style-type: none"> Make inferences and justify conclusions from sample surveys, experiments, and observational studies. Recognize the purposes of and differences among sample surveys, experiments, and observational studies <ul style="list-style-type: none"> Explain how randomization relates to each. Use data from a sample survey to estimate a population mean or proportion. Develop a margin of error through the use of simulation models for random sampling. <hr/> <ul style="list-style-type: none"> Use data from a randomized experiment to compare two treatments <ul style="list-style-type: none"> Use simulations to decide if differences between parameters are significant. Decide if a specified model is consistent with results from a given data-generating process. <ul style="list-style-type: none"> <i>For example, a model says a spinning coin falls heads up with probability 0.5. Would a result of 5 tails in a row cause you to question the model?</i> Compare theoretical and experimental results to evaluate the effectiveness of a treatment. Evaluate reports based on data.
<p>Probability</p> <p>S-MD6 S-MD7</p>	<p>Students will know that:</p> <ul style="list-style-type: none"> (+) The <u>probability</u> of an event is the chance that an event will occur and is represented by a decimal, fraction or percent with a value that falls between 0 and 1. $\text{Probability} = \frac{\text{The number of ways an event can occur}}{\text{Total number of possible outcomes}}$ <ul style="list-style-type: none"> (+) The <u>relative frequency</u> can be used as a measure of probability 	<p>Students will be able to:</p> <ul style="list-style-type: none"> (+) Extend their knowledge of probability to more complex probability models. <i>For example, situations such as those involving quality control, or diagnostic tests that yields both false positive and false negative results.</i> (+) Use probabilities to make fair decisions (e.g., drawing by lots, using a random number generator). (+) Analyze decisions and strategies using probability concepts (e.g., product testing, medical testing, pulling a hockey goalie at the end of a game)

	<p>when an event occurs a large number of times.</p> <p>Relative Frequency = $\frac{\text{Total number of times an event actually occurs}}{\text{Total number of trials}}$</p>	
	<p><u>Critical Vocabulary</u>: Statistics, Inferences, Population, Random Sampling, Mean, Standard Deviation, Normal Distribution, Data Sets, Normal Curve, Experiment, Simulation, Theoretical, Empirical, Sample Survey, Observational Study, Randomization, Margin of Error, Treatment, Parameters, (+) Fair Decisions</p>	
Common Final Exam		

Pacing Chart
UNIT 4: Inferences and Conclusions from Data

TIME FRAME	TOPIC	SUGGESTED PERFORMANCE TASKS ACTIVITIES/PROJECTS ASSESSMENTS	RESOURCES/INTERDISCIPLINARY CONNECTIONS
Mid Apr – End of Apr	Statistical Methods	3 websites that explain standard deviation http://www.youtube.com/watch?v=HvDqzbzu0i0E http://mathworld.wolfram.com/StandardDeviation.html http://davidmlane.com/hyperstat/A16252.html Video on standard deviation http://www.youtube.com/watch?v=Y2wnchUkTyQ Normal Distribution http://stattrek.com/Lesson2/Normal.aspx	Text Sections: 9-5, 9-6, 9-8 Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com
End of Apr – End of May	Data Analysis	3 websites on data collection http://nnlm.gov/evaluation/workshops/measuring_your_impact/DataCollectionHandout.pdf http://dstraub.cis.gsu.edu:88/quant/4datacoll.asp http://www.prm.nau.edu/prm447/methods_of_data_collection_lesson.htm Simulations http://classroom.jc-schools.net/basic/math-prob.html	Text Sections: (Not Supported by current textbook) Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com

End of May – Early June	Probability	Probability and experiments http://www.mathsisfun.com/data/probability.html Simulations & probability http://classroom.jc-schools.net/basic/math-prob.html Experimental probability http://www.shodor.org/interactivate/activities/ExpProbability/ 2 websites on conditional probability http://www.mathgoodies.com/lessons/vol6/conditional.html http://www.mathgoodies.com/lessons/vol6/intro_probability.html	Text Sections: 9-3 Teacher resources have activities, videos, projects, & enrichment. www.khanacademy.com www.teachertube.com exchange.smarttech.com
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